

Madde and RTSect

...or the magic of sinusoids

Svante Granqvist

Royal Institute of Technology (KTH)

Stockholm, Sweden

Outline

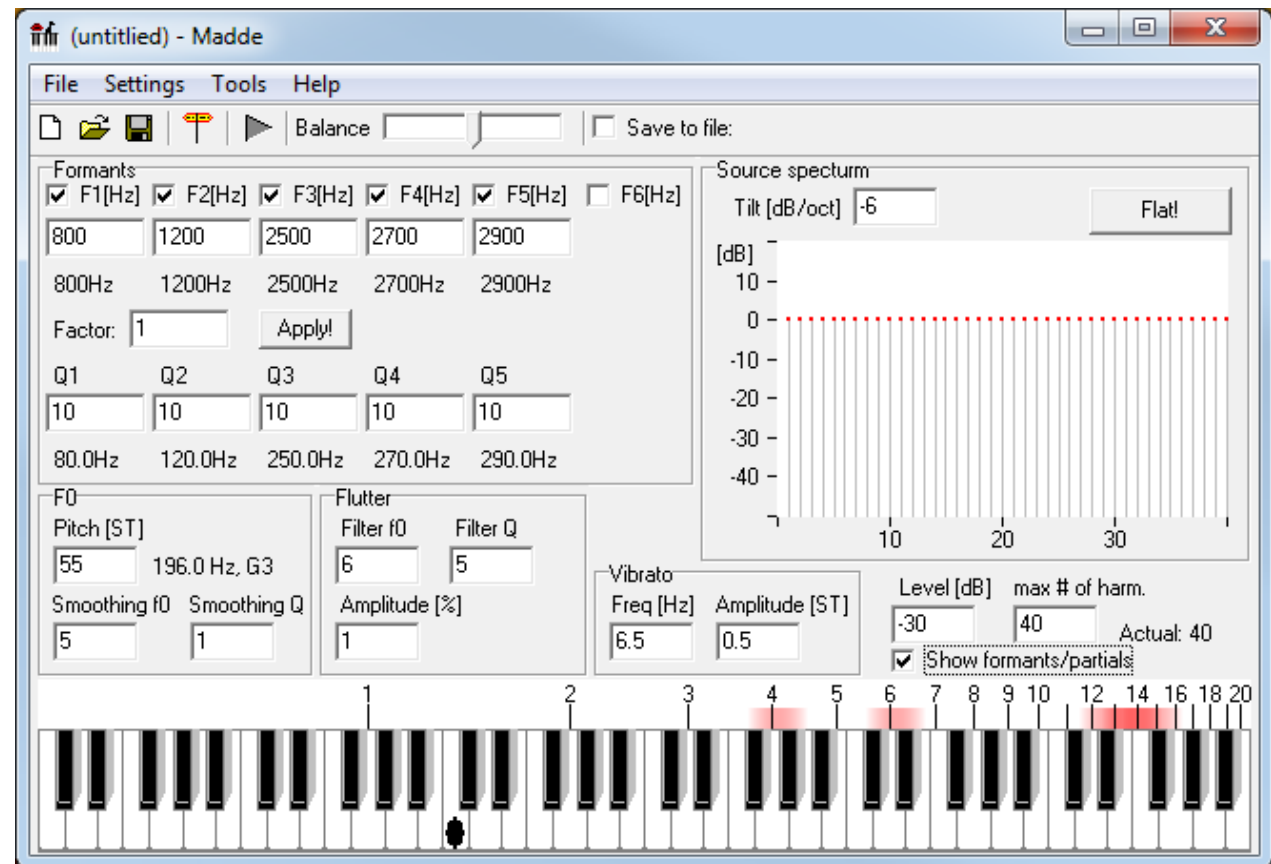
- Madde
- RTSect
- What *is* a partial, really?
 - Sinusoids, spectra, intervals, voice source
- Back to Madde and RTSect, demos and tricks

Madde

- Madde is a singing synthesiser
- Madde is written in honour to Musse, the KTH singing synthesiser from the 1970's
- Musse used an oscillator as the voice source, Madde uses additive synthesis, so that the spectrum of the voice source can be controlled in more detail
- Madde is more of a demonstrator than a research tool

Madde

- Demo

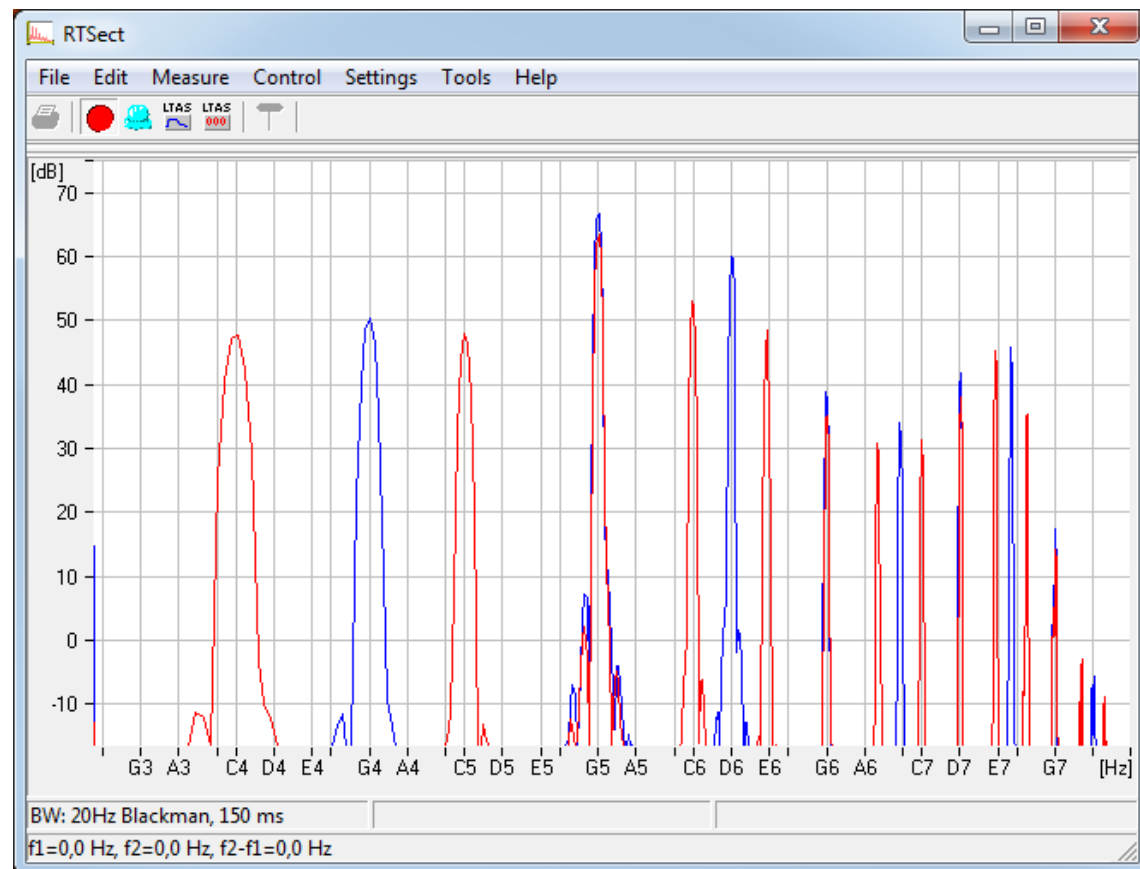


RTSect

- RTSect shows the spectrum in real time
- It can show two spectra simultaneously
- The frequency axis can be marked with tones (A4, E2 etc) instead of Hz
- Good for showing intervals, formants etc

RTSect

- Demo

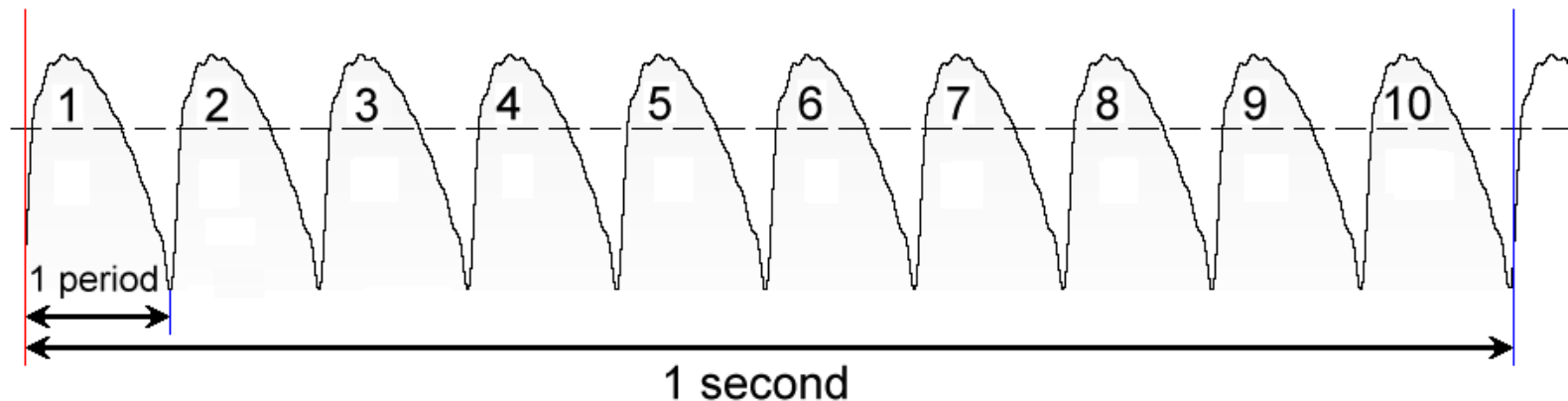


Spectrum?

- So, what *is* a spectrum, really?
- And what are partials?
- Exactly what do we mean when we say that a signal contains both low and high frequencies?
- And what *is* a frequency?

Frequency?

- Frequency means "often-ness", ie how often something happens
- So, for example this waveform repeats itself 10 times per second, so it has a frequency of 10 hertz (Hz)



Demo

- Record voice

Spectrum = Fourier analysis

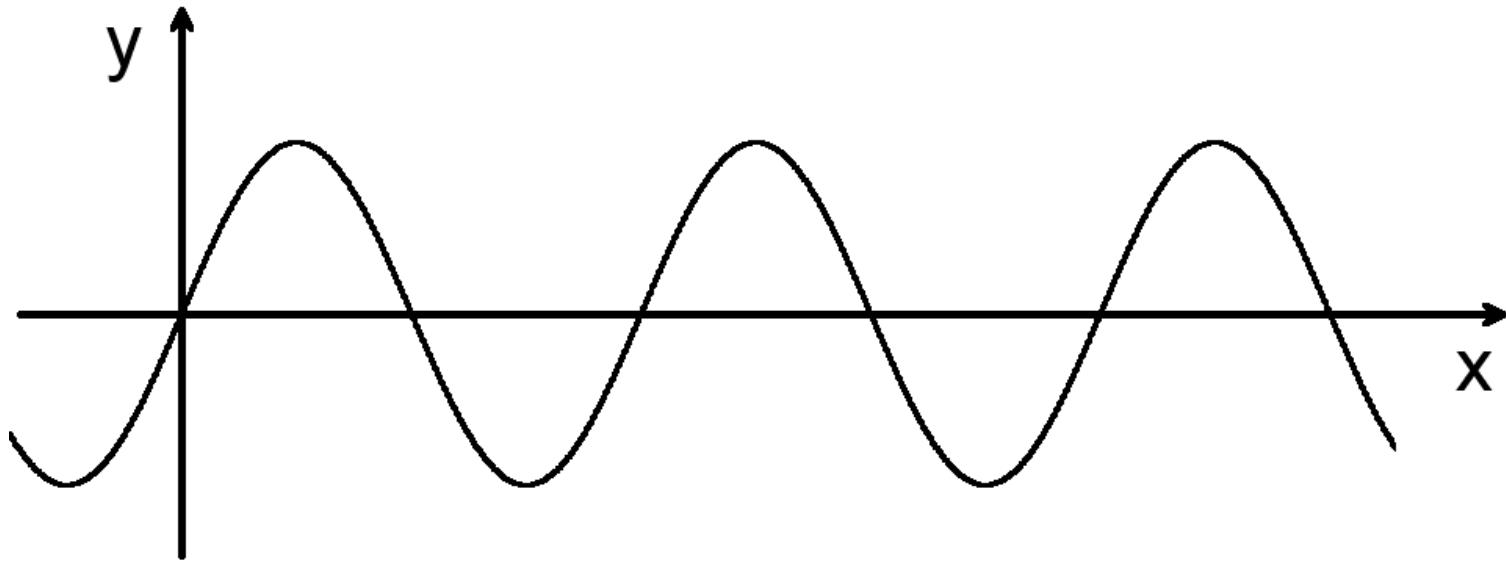
- Fourier said:
 - Give me any periodic waveform and I can describe it as a sum of sinusoids.



Jean Baptiste Joseph Fourier, 1768-1830, a french scientist

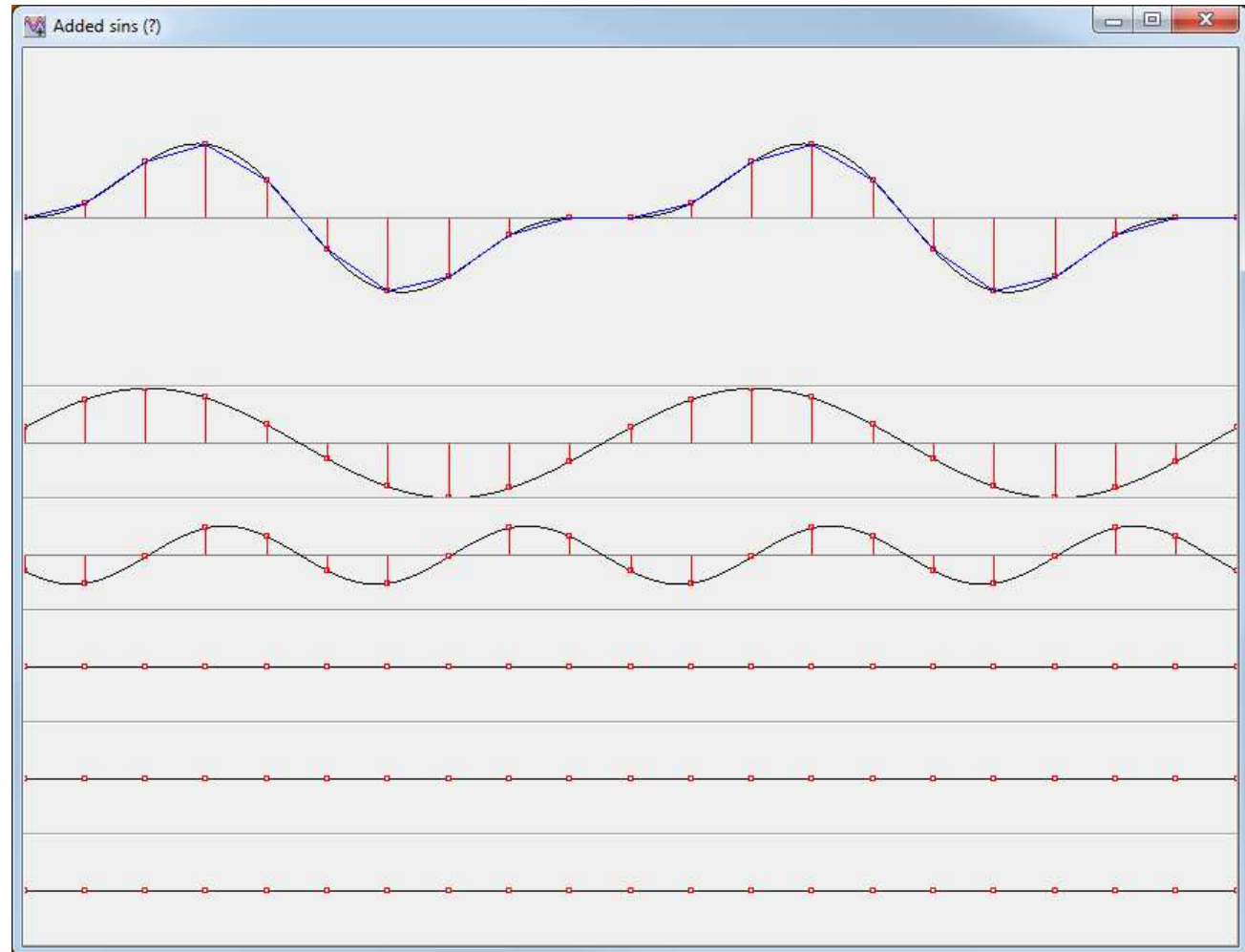
Sinusoid?

$$y = \sin(x)$$



AddSin

- Demo



Adding sinusoids

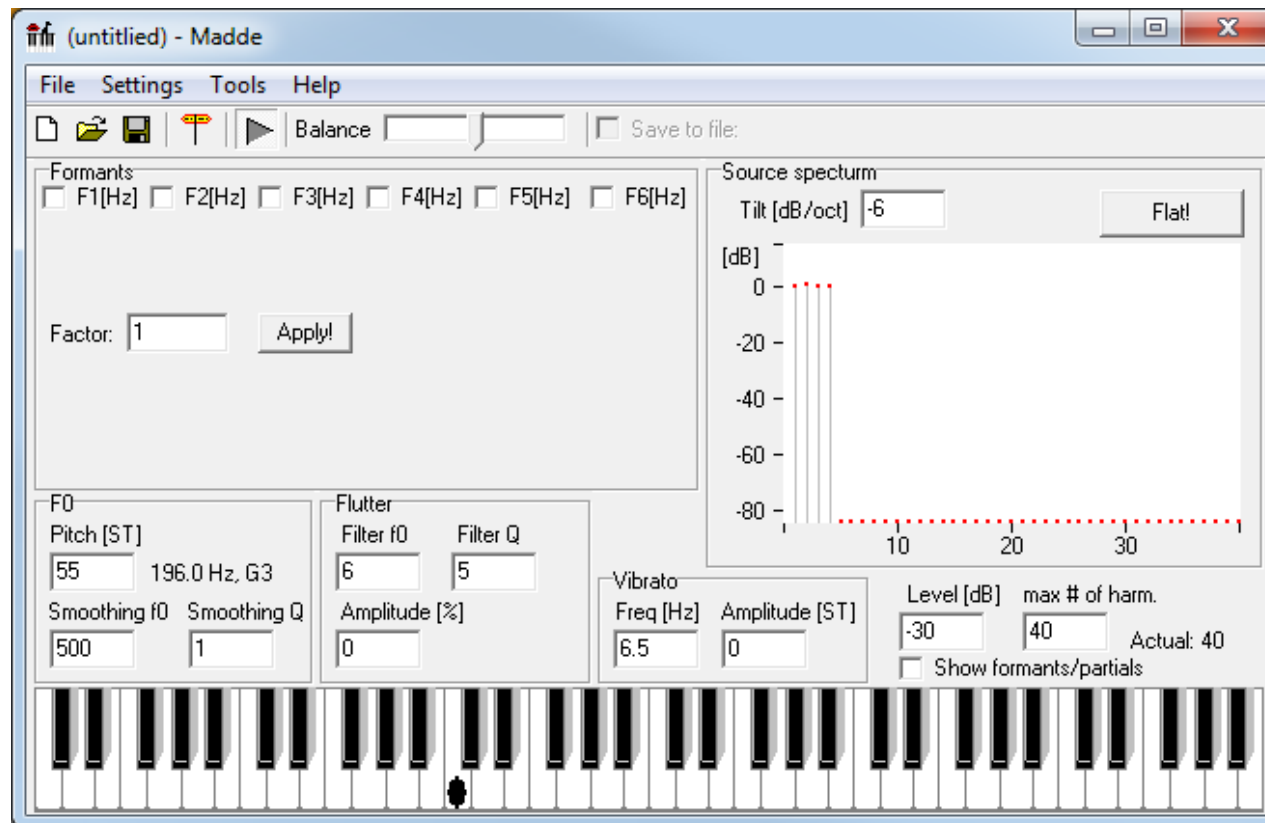
- So, by adding sinusoids we can get any waveform = any sound
- As Fourier said:
 - Give me any periodic waveform and I can describe it as a sum of sinusoids.

Spectrum

- Those sinusoids are actually the "partials" or "harmonics" that can be seen in a spectrum
- The spectrum is the signal *seen as* a sum of sinusoids

Madde

- Demo of the sound from added sinusoids



How to find the sinusoids

- That was building a waveform from sinusoids
- Can we go the other way, ie find what sinusoids that are needed to build the signal?
- Yes, RTSect does that (by Fourier analysis)

For a given waveform, how do we find the partials?

- How to find ω_p in $f(x)$:

$$\int_0^T f(x) \cdot \sin(\omega_p \cdot t) dt = \int_0^T A \sin(\omega_1 \cdot t) \cdot \sin(\omega_p \cdot t) dt = \frac{A}{2} \int_0^T (\cos((\omega_1 + \omega_p) \cdot t) + \cos((\omega_1 - \omega_p) \cdot t)) dt$$

$$\int_0^T \cos((\omega_1 + \omega_p) \cdot t) dt = 0$$

$$\int_0^T \cos((\omega_1 - \omega_p) \cdot t) dt = 0 \quad \text{if } \omega_1 \neq \omega_p$$

$$\int_0^T \cos((\omega_1 - \omega_p) \cdot t) dt = \int_0^T 1 dt = T \quad \text{if } \omega_1 = \omega_p$$

$$\int_0^T f(x) \cdot \cos(\omega_p \cdot t) dt = \int_0^T A \cos(\omega_1 \cdot t) \cdot \cos(\omega_p \cdot t) dt = \frac{A}{2} \int_0^T (-\cos((\omega_1 + \omega_p) \cdot t) + \cos((\omega_1 - \omega_p) \cdot t)) dt$$

$$\int_0^T \cos((\omega_1 + \omega_p) \cdot t) dt = 0$$

$$\int_0^T \cos((\omega_1 - \omega_p) \cdot t) dt = 0 \quad \text{if } \omega_1 \neq \omega_p$$

$$\int_0^T \cos((\omega_1 - \omega_p) \cdot t) dt = \int_0^T 1 dt = T \quad \text{if } \omega_1 = \omega_p$$

$$\int_0^T f(x) \cdot \sin(\omega_p \cdot t) dt \quad \text{and} \quad \int_0^T f(x) \cdot \cos(\omega_p \cdot t) dt$$

Use complex numbers and calculate the cosine integral in the real part and the sine integral in the imaginary part

$$\int_0^T f(x) \cdot (\cos(\omega_p \cdot t) + j \sin(\omega_p \cdot t)) dt = \int_0^T f(x) \cdot e^{j\omega_p \cdot t} dt$$

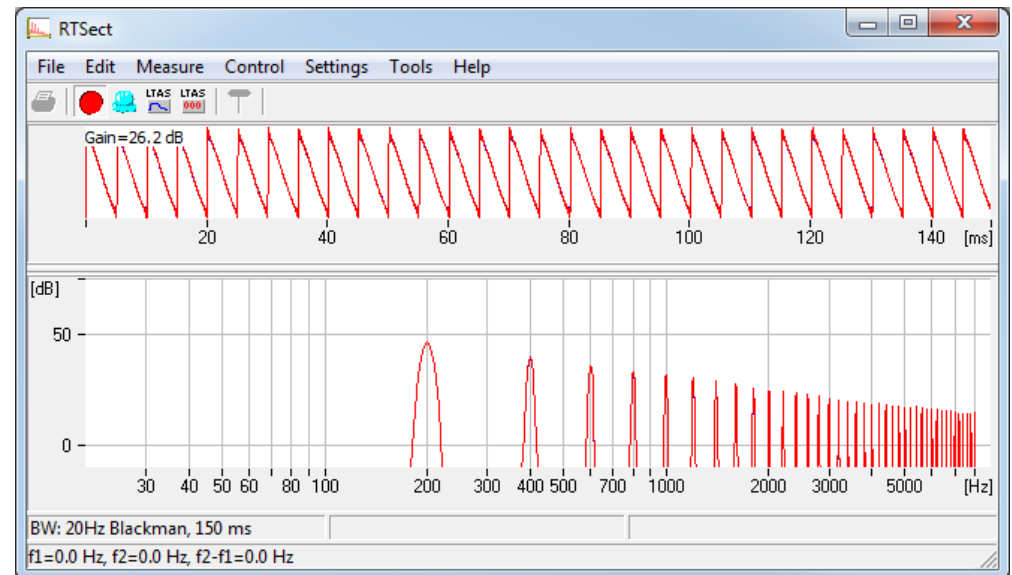
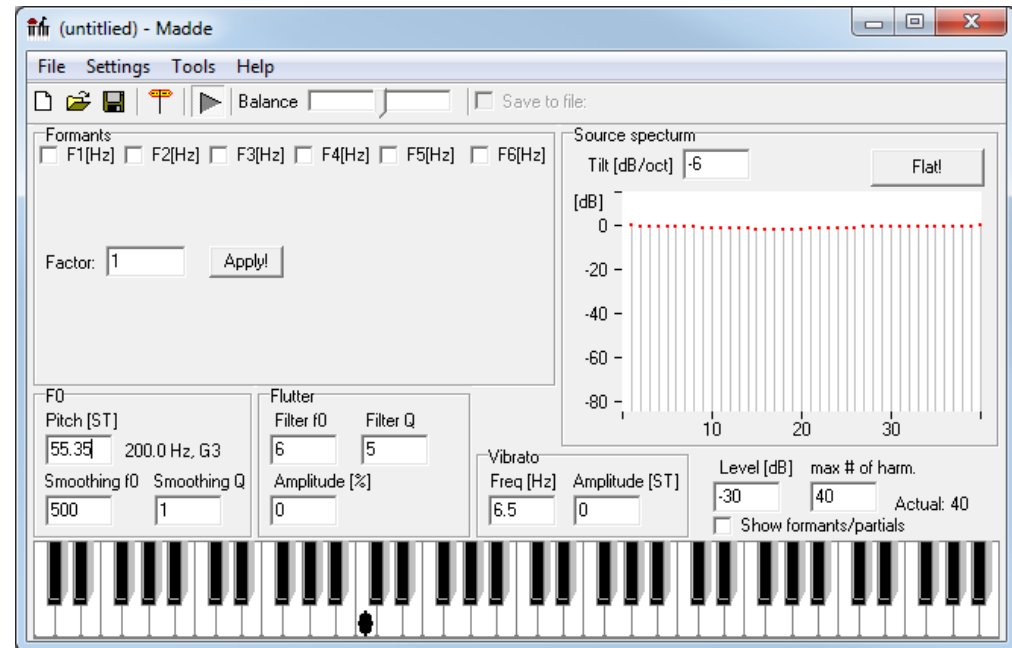
+ add some constants

RTSect

- RTSect does the Fourier analysis
 - It shows the partials of a sound

RTSect

- Demo of partials

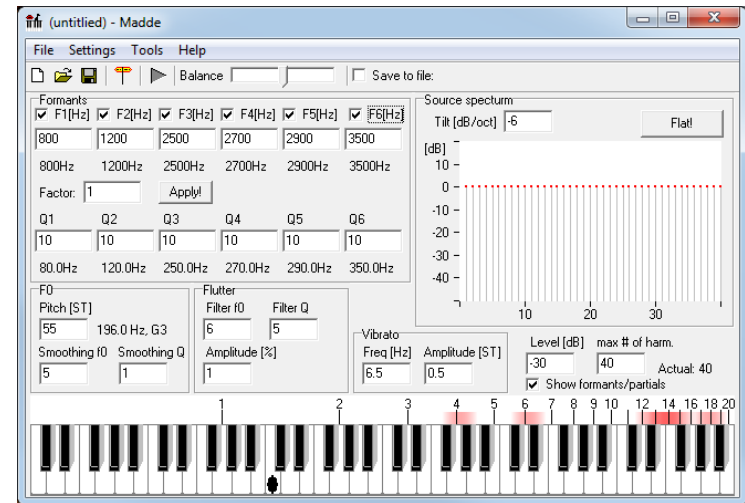


Madde + RTSect

- Partialals
- Formants
- 2x Madde – intervals

Madde

- Demo of
 - Formants
 - Throat lengthening
 - Vibrato
 - Flutter
 - Partial/formant matching



RTSect

- Demo of
 - Single/dual channels
 - Frequency axes
 - Bandwidth

